## Answers to Final Examination

The complete histogram of percentage grades looks like this:

| $\mathrm{N}=29$ |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Mean $=67.0$ |  |  |  |  |  |  |  |  |  |  |  |  |
| Median $=72$ |  |  |  |  | 66 |  |  |  | 89 |  | 97 |  |
|  | 38 |  | 54 |  | 66 | 73 |  |  | 88 |  | 96 |  |
|  | 38 |  | 53 |  | 65 | 72 |  | 82 | 86 |  | 95 |  |
| 18 | 35 | 43 | 51 | 63 | 65 | 70 | 75 | 80 | 86 | 90 | 95 | 100 |

You can determine your letter grade by looking up the score in the following table:

| Range | Grade | N |
| :---: | :--- | :--- |
| $95-100$ | $\mathrm{~A}+$ | 5 |
| $84-94$ | A | 5 |
| $77-83$ | $\mathrm{~A}-$ | 2 |
| $73-76$ | $\mathrm{~B}+$ | 2 |
| $65-72$ | B | 6 |
| $61-64$ | $\mathrm{~B}-$ | 1 |
| $57-60$ | $\mathrm{C}+$ | 0 |
| $47-56$ | C | 3 |
| $43-46$ | $\mathrm{C}-$ | 1 |
| $25-42$ | D | 3 |
| $00-24$ | NP | 1 |

## Problem 1—Short answer (10 points)

1a) The enigma function implements the algorithm credited to the Greek mathematician Eratosthenes ( $3^{\text {rd }}$ century BCE) for determining prime numbers, which is generally called the Sieve of Eratosthenes. The $k^{\text {th }}$ element of the returned array has the value true if $k$ is prime. The result of calling enigma (16) is therefore

| F | F | T | T | F | T | F | T | F | F | F | T | F | T | F | F |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |

1b) The value produced by the outer call to mystery is the string "314159"; the quotes would not be printed in this problem but were accepted for the exam.

Problem 2—Simple graphics (15 points)

```
/*
    * Creates a GCompound consisting of a rectangular frame that contains
    * a set of GLabel objects, one for each line in the string array lines.
    */
function createTextBox(lines, font) {
    var labels = [];
    var width = 0;
    for (var i = 0; i < lines.length; i++) {
        var label = GLabel(lines[i]);
        label.setFont (font);
        if (label.getWidth() > width) width = label.getWidth();
        labels.push(label);
    }
    width += 2 * TEXT_MARGIN;
    var height = 2 * TEXT_MARGIN + labels.length * labels[0].getHeight();
    var frame = GRect(0, 0, width, height);
    var textBox = GCompound();
    textBox.add (frame);
    var y = TEXT_MARGIN + labels[0].getAscent();
    for (var i = 0; i < labels.length; i++) {
        textBox.add(labels[i], TEXT_MARGIN, y);
        y += labels[i].getHeight();
    }
    return textBox;
}
```

Problem 3-Interactive graphics ( 20 points)

```
/*
    * Simulates the arcade game of Whac-A-Mole in which a circle turns
    * black at random intervals and the user has to click on that circle
    * before it turns white again. Clicking on a black circle removes it
    * from the window.
    */
function WhacAMole() {
        var gw = GWindow(GWINDOW_WIDTH, GWINDOW_HEIGHT);
        createCircles(gw);
        var circle = null;
        var timeStep = function() {
            var x = randomInteger(0, GWINDOW_WIDTH);
            var y = randomInteger(0, GWINDOW_HEIGHT);
            if (circle !== null) circle.setFilled(false);
            circle = gw.getElementAt (x, y);
            if (circle !== null && !circle.isFilled()) {
                circle.setFilled(true);
            }
        };
        var clickAction = function(e) {
            var obj = gw.getElementAt(e.getX(), e.getY());
            if (obj !== null && obj.isFilled()) {
                gw.remove(obj);
                circle = null;
            }
        };
        var timer = setInterval(timeStep, TIME_STEP);
        gw.addEventListener("click", clickAction);
}
/*
    * Creates the pattern of circular holes on the graphics window. The
    * circles form a square matrix with N_CIRCLES_PER_ROW in each row
    * and column. The diameter of each circle is given by the constant
    * CIRCLE_SIZE and the space between each circle is given by the
    * constant CIRCLE_SEP.
    */
function createCircles(gw) {
    var delta = CIRCLE_SIZE + CIRCLE_SEP;
    for (var i = 0; i < N_CIRCLES_PER_ROW; i++) {
            var y = CIRCLE_SEP / 2 + i * delta;
            for (var j = 0; j < N_CIRCLES_PER_ROW; j++) {
                var x = CIRCLE_SEP / 2 + j * delta;
                var hole = GOval(CIRCLE_SIZE, CIRCLE_SIZE);
                gw.add(hole, x, y);
            }
    }
}
```


## Problem 4—Strings (15 points)

```
/*
    * Generates a random permutation suitable for use as a reflector. The
    * conditions necessary to be a reflector are (1) that no letter maps to
    * itself and (2) the permutation is symmetric so that if A maps to B,
    * B must map to A.
    */
function generateRandomReflector() {
        var candidates = ALPHABET;
        var reflector = STARTER;
        var base = "A".charCodeAt (O);
        while (candidates.length > 0) {
            var c1 = candidates.charAt (0);
            candidates = candidates.substring(1);
            var i = randomInteger(0, candidates.length - 1);
            var c2 = candidates.charAt(i);
            candidates = candidates.substring(0, i) + candidates.substring(i + 1);
            reflector = replaceCharAt (reflector, c2.charCodeAt(0) - base, c1);
            reflector = replaceCharAt (reflector, c1.charCodeAt (0) - base, c2);
        }
        return reflector;
}
/*
    * Returns a new string in which the character at the specified index in
    * str is replaced by ch.
    */
function replaceCharAt(str, index, ch) {
    return str.substring(0, index) + ch + str.substring(index + 1);
}
```


## Problem 5—Arrays (10 points)

```
/*
    * Finds and returns the first element in the array that appears
    * more than once in the array. If no duplicated element exists,
    * findDuplicate should return the value null.
    */
function findDuplicate(array) {
    for (var i = 0; i < array.length; i++) {
            if (array.indexOf(array[i], i + 1) !== -1) {
            return array[i];
            }
    }
    return null;
}
```

If you didn't think of using indexOf, the same functionality is easy to achieve using a helper function.

Problem 6-Data structures (20 points)

```
/*
    * Prints a cheat sheet for the Adventure game showing the name of each
    * object, its short description in parentheses, and the short description
    * of its initial location. After each object in the list, the
    * printCheatSheetForObjects function goes through the rooms data
    * structure and print out a line for each entry in which that object
    * acts as a key to a locked passage.
    */
function printCheatSheetForObjects(objects, rooms) {
        for (var objectName in objects) {
            var obj = objects[objectName];
            var desc = obj.getDescription();
            var loc = obj.getInitialLocation();
            if (loc !== "PLAYER") {
                    loc = rooms[loc].getShortDescription();
            }
            console.log(objectName + " (" + desc + ") starts: " + loc);
            for (var roomName in rooms) {
                var room = rooms[roomName];
                var motionTable = room.getMotionTable();
                    for (var i = 0; i < motionTable.length; i++) {
                    var entry = motionTable[i];
                    if (objectName === entry.getKeyName()) {
                        var dir = entry.getDirection();
                                var short = room.getShortDescription();
                                console.log(" Needed for " + dir + " from " + short);
                    }
                }
            }
        }
}
```

Problem 7-Reading data structures from files (15 points)

```
/* Constants */
const STECKERBOARD_PAIRS = 4;
/*
    * Reads a data file into an internal data structure for the Enigma
    * codebook. Each line of the data file has the form
        <date> <order> <setting> <stecker>
    where the individual components of the line have the following values:
    *
    * - <date> is the date, written as a string (without the quotes).
    * - <order> is the rotor order, written as a three-digit integer.
    * - <setting> is the rotor setting, written as three letters.
    * - <stecker> is a sequence of letter pairs separated by spaces.
    The result of calling readEnigmaCodebook is a map in which the keys
    are dates and the values are aggregates with the fields rotorOrder,
    rotorSetting, and steckerPairings. The rotorOrder field is an
    integer, the rotorSetting field is a string, and the steckerPairings
    field is an array of two-letter strings.
    */
function readEnigmaCodebook(filename) {
    var lines = File.readLines(filename);
    var codebook = { };
    var line = lines.shift();
    while (line !== undefined) {
        var space = line.indexOf(" ");
        var date = line.substring(0, space);
        var entry = { };
        var start = space + 1;
        space = line.indexOf(" ", start);
        entry.rotorOrder = parseInt(line.substring(start, space));
        start = space + 1;
        space = line.indexOf(" ", start);
        entry.rotorSetting = line.substring(start, space);
        entry.steckerPairing = [ ];
        start = space + 1;
        for (var i = 0; i < STECKERBOARD_PAIRS; i++) {
            space = line.indexOf(" ", start);
            if (space === -1) space = line.length;
            entry.steckerPairing.push(line.substring(start, space));
            start = space + 1;
        }
        codebook[date] = entry;
        line = lines.shift();
    }
    return codebook;
}
```

